

$$\frac{dN}{dt} = -N_m(t)\beta_m + Y_m + \sum N_k(t)Y_{k-m}$$